



INSTITUT D'OPTIQUE GRADUATE SCHOOL

Wave particle duality for a single photon: from Einstein light quanten to Wheeler's delayed choice experiment

Lausanne, 12 mars 2009

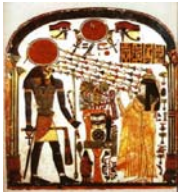
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### Light across ages: wave or particle?


Antiquity (Egypt, Greece): **particles towards or from the eye** (Epicure, Aristotle, Euclid)




Middle age, renaissance: **engineering**: corrective glasses, telescope (Al Hazen, Bacon, Leonardo da Vinci, Galilée, Kepler...)



XVII<sup>th</sup> cent.: **Waves** (as "riddles on water") Huyghens





Newton (Opticks, 1702): **particles** (of various colours)




### XIX<sup>th</sup> cent. The triumph of waves


Young, Fresnel (1822): **interference, diffraction, polarisation**: light is a **transverse wave**

Maxwell (1870): light is an **electro-magnetic wave**





1900: "Physics is completed" (Lord Kelvin) ... except for two details!??



### Early XX<sup>th</sup>: Photons (particles come back)

- Einstein (1905). **Light made of quanta**, elementary grains of energy  $E = h\nu$  and momentum  $p = h\nu/c$  (named "photons" in 1926 only).
- Quantitative predictions for the photoelectric effect
- Ideas not accepted until Millikan's experiments on photoelectric effect (1915).
- Nobel award to Einstein (1922) for the photoelectric effect
- Compton's experiments (1923): momentum of photon in the X ray domain

How to reconcile the particle description with typical wave phenomenon of diffraction, interference, polarisation? Particle or wave?

### Wave particle duality

Einstein 1909 Light is **both waves** (capable to interfere) and an **ensemble of particles** with defined energy and momentum...

Blackbody radiation fluctuations

$$\bar{\varepsilon}^2 = \left( h\nu\rho + \frac{c^3\rho^2}{8\pi\nu^2} \right) d\nu$$

Random particles ("shot noise")      Random waves ("speckle")

Louis de Broglie 1923

Similarly **particles such as electrons** behave like a **wave** (diffraction, interference)

$$\lambda = \frac{h}{p}$$



Easy to say the words, but difficult to represent by images

### Wave particle duality: fruitful

A very successful **concept at the root of the quantum revolution**:

- Understanding the structure of **matter**, its properties, its interaction with **light**
  - Stability of atoms, molecules, solids
  - Electrical, mechanical, thermal properties
  - Spectroscopic properties
- Understanding "exotic properties"
  - Superfluidity, superconductivity, BEC
- Inventing **new devices**
  - Laser, transistor

Quantum mechanics applied to large ensembles

How does it work for a single particle? See textbooks (e.g. Feynman)

### Wave particle duality in textbooks wave-like behaviour for particles

Particles emitted one at a time, all "in the same state" (same origin, direction distribution, energy)

When detector D moves,  $P_D$  is modulated

When a hole is closed no modulation ( $P_D$  constant)

Interpretation: each particle is described by a wave passing through both holes and recombining on the detector.

$P_D$  depends on the path difference  $\Delta = SH_1D - SH_2D$

### Wave-like behavior with faint light?

Taylor	1909	Diffraction	Photographic plate	Oui
Dempster & Batho	1927	Grating, Fabry-Perot	Photographic plate	Oui
Janossy and Naray	1957	Michelson interferom.	Photomultiplier	Oui
Griffiths	1963	Young slits	Intensifier	Oui
Dontsov & Baz	1967	Fabry-Perot	Intensifier	NON
Scarl et al.	1968	Young slits	Photomultiplier	Oui
Reynolds et al.	1969	Fabry-Perot	Intensifier	Oui
Bozec, Imbert et al.	1969	Fabry-Perot	Photographic plate	Oui
Grishaev et al.	1971	Jamin interferometer	Intensifier	Oui
Zajonc et al.	1984	Fiber interferometer, delayed choice	Photomultiplier	Oui
Alley et al.	1985	Fiber interferometer, delayed choice	Photomultiplier	Oui

Average distance between photons large compared to interferometer size

Single particle interference?

### How to know one has single particles? The "which path" Gedankenexperiment

Particles emitted one at a time, all "in the same state" (same origin, direction distribution, energy)

Singles detection  $P_1 \neq 0$

Coincidences detection  $P_C = 0$

Singles detection  $P_2 \neq 0$

$D_1$  et  $D_2$  observe random pulses, with a constant mean rate, but no coincidence ( $P_C = 0$ ): anticorrelation

$P_C = 0$ : a single particle passes either through  $H_1$ , or through  $H_2$ , not through both paths simultaneously. A single particle cannot be split.

Opposite behavior predicted for a wave:  $P_C \neq 0$

### The which path GedankenExperiment

Particles emitted one at a time

Singles detection  $P_1 \neq 0$

Coincidences detection  $P_C = 0$

Singles detection  $P_2 \neq 0$

Not realized before 1985

- Particle nature considered "obvious" for electrons, neutrons, atoms, molecules: only wave-like effects searched
- Case of faint light: particle like behaviour considered "obvious" when the average distance between photons is large: only wave-like effects searched with very attenuated light

### The particle-like character of faint light is not proved by photoelectric effect

Photoelectric effect fully interpretable by the semi-classical model of photo-ionization (Lamb and Scully, 1964)

- Quantized detector with a ground state and a continuum of excited states (atom, molecule, metal ...)
- Light: classical electromagnetic field
- Fermi golden rule: rate of photo ionization proportional to density of final states

Remark: in 1905 (eight years before Bohr's atom) no quantum model, neither for light nor for matter: photoelectric effect impossible to understand in classical physics. Einstein chose to quantize light. He could have chosen to quantize matter.

### According to modern quantum optics faint light is not made of single particles

Attenuated light described as a Glauber quasi-classical state, which has the same behavior as a classical electromagnetic wave.

If one insists for speaking of particles: in any interval of time, or space volume, probabilistic distribution of particles

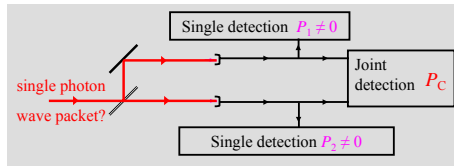
$P(1)$  small but  $P(2) \sim P(1)^2$

Probability to have two particles never zero. No anticorrelation expected between two detectors:  $P_C \neq 0$

Are there means to produce single photon states of light?  
Can we demonstrate experimentally single particle behavior?

## A beam-splitter to discriminate between a particle-like and a wave-like behaviour

(AA, Philippe Grangier, 1985)



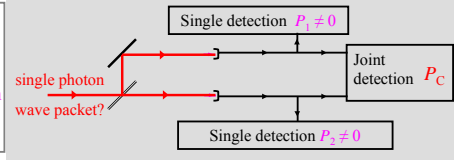
Single particle: one expects  $P_c = 0$

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## Wave-like behaviour at a beam splitter

(AA, Philippe Grangier, 1985)

Wave split in two at BS: one expects joint detection  $P_c \neq 0$



More precisely, joint photodetection probability proportional to **mean square** of wave intensity  $P_c = \eta^2 RT \bar{I}^2$

$$\text{but } \overline{I^2} \geq (\overline{I})^2$$

while  $P_1 = \eta R \bar{I}$ ,  $P_2 = \eta T \bar{I}$

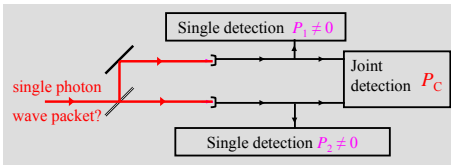
for a wave  $\alpha = \frac{P_c}{P_1 P_2} \geq 1$

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## A quantitative criterion to discriminate wave-like vs. particle-like behaviour

Particle: one expects  $P_c = 0$

Wave: one expects  $P_c > P_1 P_2$



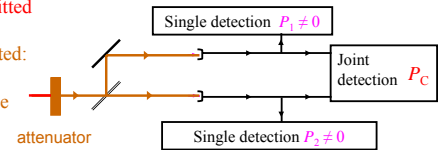
Criterion for a particle like behaviour:  $\alpha = \frac{P_c}{P_1 P_2} < 1$  PG, AA, 1985

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## Faint light does not pass single particle test

(AA, Philippe Grangier, 1985)

Light pulses emitted by a LED and strongly attenuated: 0,01 photon per pulse, on average



Experimental result:  $\alpha_{\text{meas}} = 1.07 \pm 0.08$  not single particle behaviour

In agreement with classical description of wave splitting.

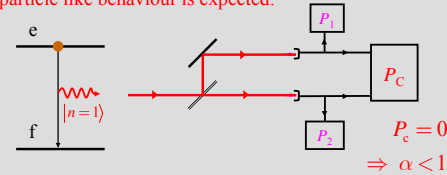
Quantum optics: faint light described as a quasi classical "coherent" state. Number of photons is not a "good quantum number"; Poisson distribution:  $P(2) \sim P(1)^2 \neq 0$  just enough to explain coincidences

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## Single photon sources

Quantum optics allows us to design **sources of single photons** ( $|n=1\rangle$ ) for which a **particle like behaviour** is expected:

Isolated excited atom  
Emits one and only one photon



In **classical light sources** (thermal radiation, fluorescence lamp) **many atoms simultaneously excited**: Poisson distribution (laser also)

To obtain single photons effects, isolate a single atom emission:

- in space (Kimble, Dagenais, Mandel, antibunching)
- in time (J Clauser 1974, non classical effects in radiative cascade; AA, PG, heralded single photon,  $\alpha < 1$ )

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## Isolating single photons emitters in time

(AA, Philippe Grangier, 1985)

Assembly of atoms emitting  $10^7 \text{ s}^{-1}$  pairs of photons. In the 5 ns time window following detection of  $v_1$ , only one atom is likely to emit a photon  $v_2$  (cf J Clauser, 1974).



Experimental result:

$$\alpha_{\text{meas}} = 0.18 \pm 0.06$$

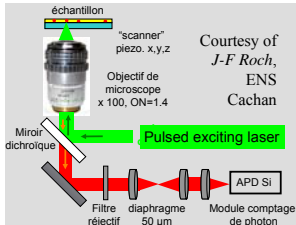
Clear anticorrelation ( $\alpha < 1$ )

Particle-like behaviour

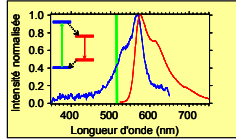
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## Modern sources: single photons emitters isolated in space and time

Isolated 4-level emitter + pulsed excitation (Lounis & Moerner, 2000)



Courtesy of  
J-F Roch,  
ENS  
Cachan



V. Jacques et al., EPJD 35, 561 (2005)

### Experimental result

$$\alpha_{\text{meas}} = 0.132 \pm 0.001$$

Clear anticorrelation ( $\alpha < 1$ )

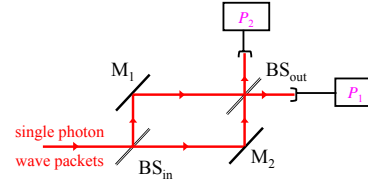
Particle-like behaviour

For a review: B. Lounis and M. Orrit,  
Rep. Prog. Phys. 68, 1129 (2005).  
P. Grangier and I. Abram,  
Phys. World, Feb. 2003

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## Single photon interference?

Can we observe interference with single photon wave packets ( $\alpha < 1$ )?

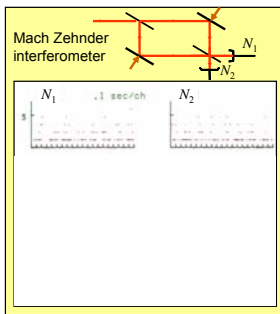


Do probabilities  $P_1$  and  $P_2$  vary (sinusoidally) when one varies the path difference?

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## Single photon interference

Interferometer with single photon source at input



Vary path difference and stay  
0.1 second at each position

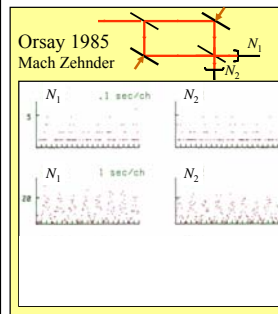
Not much to see!

Grangier, AA, 1985

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## Single photon interference

Interferometer with single photon source at input



Vary path difference and stay  
1 second at each position

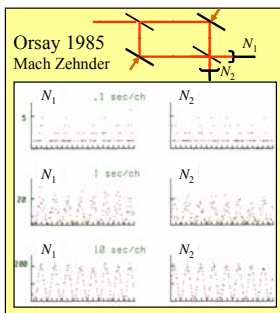
Clear modulation!

Grangier, AA, 1985

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## Single photon interference

Interferometer with single photon source at input



Vary path difference and stay  
10 seconds at each position

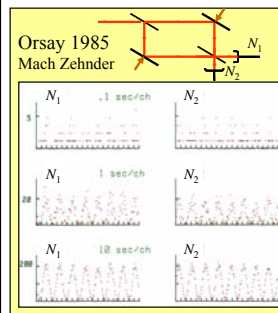
Sinusoidal variation!  
Remarkable signal to noise  
ratio, visibility close to 1.

Unambiguous wave like behaviour

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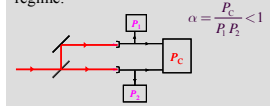
## Single photon interference

Interferometer with single photon source at input



Vary path difference and stay  
10 seconds at each position

Experiment done in the single photon  
regime:



$$\alpha = \frac{P_c}{P_1 P_2} < 1$$

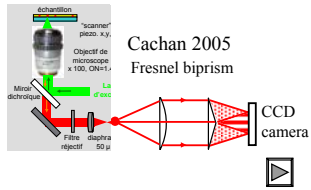
Sinusoidal variation!  
Remarkable signal to noise  
ratio, visibility close to 1.

Unambiguous wave like behaviour in the single photon regime

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## Single photon interference

A more modern implementation (Cachan, 2005)



Anticorrelation in detectors D1 and D2:  $\langle n_1 n_2 \rangle = 0.132 \pm 0.001$   
interference fringes' photon behaviour

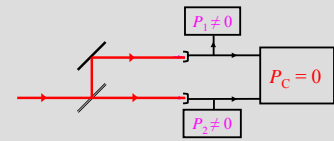
Unambiguous wave like behaviour in the single photon regime

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## Wave particle duality for single particles

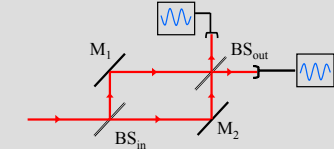
First experiment

Particle like behaviour: goes either to one side, or the other, not both.



Second experiment

Wave like behaviour: goes through both paths (output depends on paths difference)



Same single photon wave packets, same beamsplitter, contradictory images

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## To comfort oneself: Bohr's complementarity

The two experiments are incompatible. One must choose the question:

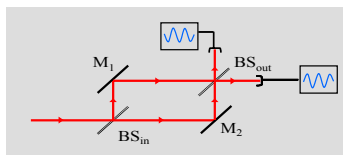
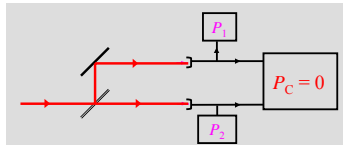
- Which way ?
- Interference ?

The two questions cannot be asked simultaneously

Could it be that the photon behaves according to the question?

What would happen if the question was chosen after passage at the input beamsplitter? Wheeler's delayed choice experiment.

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## Wheeler's delayed choice experiment

The two experiments are incompatible. One must choose the question:

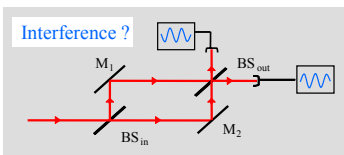
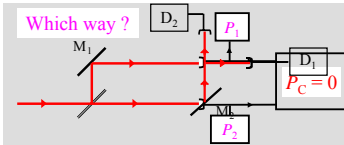
- Which way ?
- Interference ?

Slightly modify the "which way" experiment

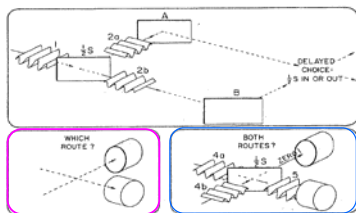
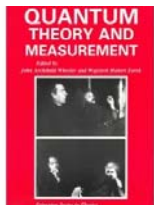
One can choose the question by introducing or removing  $BS_{out}$

One can make the choice after the photon passed  $BS_{in}$

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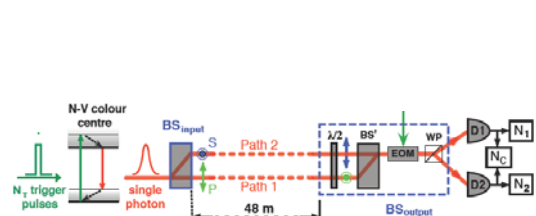
## Wheeler's proposal (1978)



The choice of introducing or removing the second beamsplitter must be space like separated from the passage at first beamsplitter, so when the photon passes the first beam splitter it cannot know which measurement will be done.

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## Experimental realization (ENS Cachan)

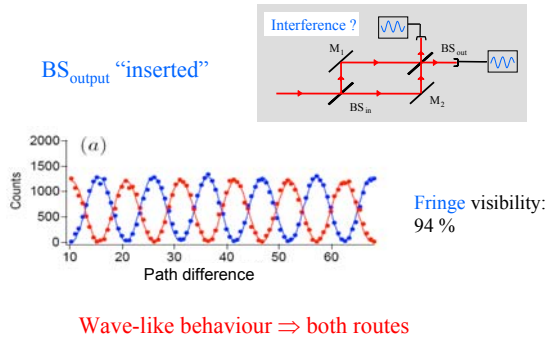


Electro Optical Modulator:   
• no voltage =  $BS_{output}$  removed  
•  $V_\pi$  =  $BS_{output}$  recombines the beams

The choice is made by a quantum random noise generator, after the photon passes the first beam splitter.

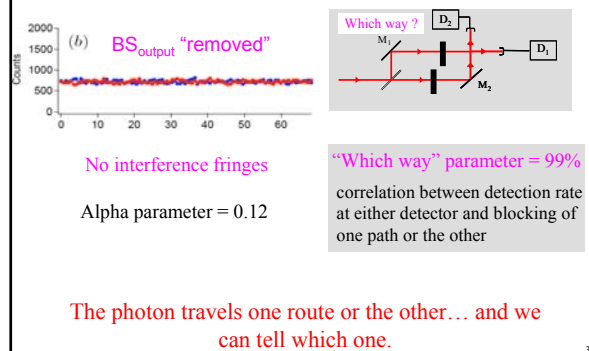
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## Delayed choice experiment: results



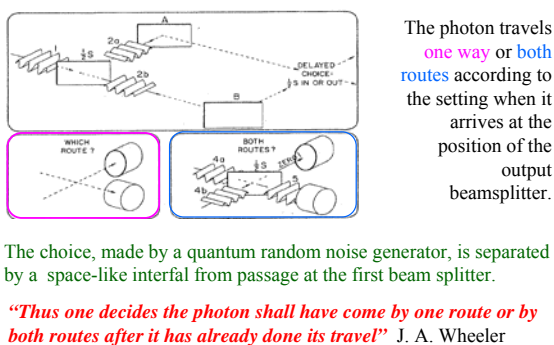
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## Delayed choice experiment: results



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## Delayed choice experiment: conclusion



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## Wave particle duality: one of the "great mysteries" of quantum mechanics

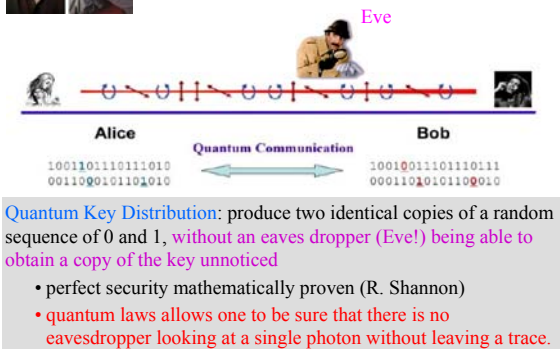
Experimental facts force us to accept it. Impossible to reconcile with images coming from our macroscopic world. To comfort ourselves:

- Quantum optics formalism gives a coherent account of it (one has not to choose one image or the other).
- Bohr's complementarity allows one to avoid too strong inconsistencies but...
- The delayed choice experiment shows that complementarity should not be interpreted in a too naïve way.

Questioning the foundations of quantum mechanics is not only an academic issue. It has led to the development of **quantum information**, i.e. **quantum cryptography** and **quantum computing**.

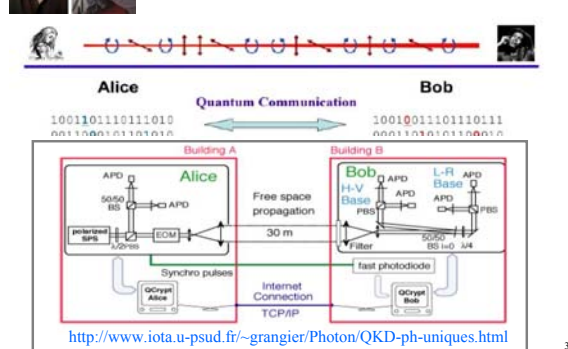
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## Quantum cryptography with single photons (BB84)



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## Quantum cryptography with single photons (BB84)



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## Cryptographie quantique: Schéma BB84 avec photon unique

Groupe d'Optique Quantique de l'Institut d'Optique (P. Grangier)

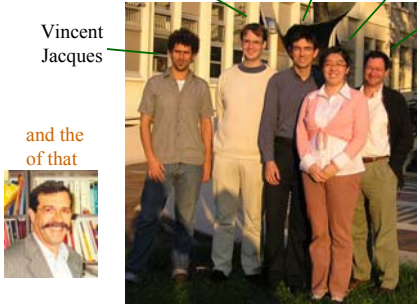


Laboratoire de photonique ENS Cachan (J F Roch)

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## Delayed choice experiment: the team

Frederic Groshans, François Treussart, E Wu, Vincent Jacques, Jean-François Roch



and the of that

god fathers experiment

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## Delayed choice experiment: one of the two big quantum mysteries (Feynman, 1960, 1982)

### Single particle interference experiment (1 particle)

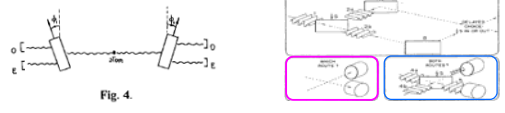
In this chapter we shall tackle immediately the basic element of the mysterious behavior in its most strange form. We choose to examine a phenomenon which is impossible, *absolutely* impossible, to explain in any classical way, and which has in it the heart of quantum mechanics. In reality, it contains the *only* mystery.

### EPR correlation (2 entangled particles)

I've entertained myself always by squeezing the difficulty of quantum mechanics into a smaller and smaller place, so as to get more and more worried about this particular item. It seems to be almost ridiculous that you can squeeze it to a numerical question that one thing is bigger than another. But there you are—it is bigger than any logical argument can produce, if

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## Delayed choice experiment: one of the two big quantum mysteries (Feynman, 1960, 1982)



### EPR correlation (2 entangled particles)

- No local realistic description (violation of Bell's inequalities)
- Bohm's hidden variables description is non-local

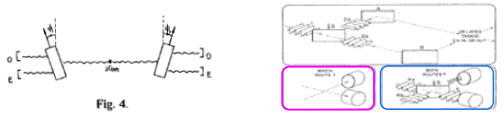
### Wheeler's delayed choice experiment (1 particle)

- Local realistic description possible (Bohm's hidden variables)

Wave-particle duality (one particle) is not as big a mystery as entanglement (elementary many-body problem)

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## Delayed choice experiment: one of the two big quantum mysteries (Feynman, 1960, 1982)



### Wheeler's delayed choice experiment (1 particle)

### EPR correlation (2 entangled particles)

Are they "only" academic (epistemological) questions?

Studies of these questions have led to the development of quantum information: quantum computing (based on entanglement) and quantum cryptography (based on single photons or entanglement)

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